Vehicle-to-Vehicle Communication: Fair Transmit Power Control for Safety-Critical Information

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Abstract—Direct radio-based vehicle-to-vehicle communication can help to prevent accidents by providing accurate and up-to-date local status and hazard information to the driver. In this paper, we assume that two types of messages are used for traffic safety-related communication: periodic messages (‘beacons’) sent by all vehicles to inform their neighbors about their current status (i.e., position), and event-driven messages sent whenever a hazard has been detected. In IEEE 802.11 DCF-based vehicular networks, interferences and packet collisions can lead to failure of reception of safety-critical information, particularly when the beaconing load leads to an almost saturated channel as it could easily happen in many critical vehicular traffic conditions. In this paper we demonstrate the importance of transmit power control for avoiding saturated channel conditions and ensuring best use of the channel for safety-related purposes. We propose a distributed transmit power control method based on a strict fairness criterion, D-FPAV, to control the load of periodic messages on the channel. The benefits are twofold: i) bandwidth is made available for higher priority data like dissemination of warnings; ii) beacons from different vehicles are treated with ‘equal rights’ and best possible reception under the available bandwidth constraints is ensured. We formally prove the fairness of the proposed approach. Then we make use of the ns-2 simulator significantly enhanced by realistic highway mobility patterns, improved radio propagation and receiver models, and the IEEE 802.11p specifications, to show the beneficial impact of D-FPAV for safety-related communications. We finally put forward a method, EMDV, for fast and effective multi-hop information dissemination of event-driven messages and show that EMDV benefits of the beaconing load control provided by D-FPAV with respect to both probability of reception and latency.

Index Terms—Vehicle-to-vehicle communication, active safety, power control, fairness, information dissemination, contention.

I. INTRODUCTION

Direct vehicle-to-vehicle communication based on radio technologies represents a key component for improving safety on the roads. Various public and private organizations around the world are funding national and international initiatives devoted to vehicular networks, such as the InternetITS Consortium [1] in Japan, the Vehicle Infrastructure Initiative (VII) [2] in the USA, the Car2Car Communication Consortium (C2CCC) [3] in Europe and the Network on Wheels project (NoW) [4] in Germany, to name a few. Currently, the IEEE 802.11p working group [5] is developing a standard based on carrier-sense multiple access (CSMA) and tailored to vehicular environments. The effort is assisted by initiatives from various parts of the globe.

Direct radio-based vehicle-to-vehicle communication can provide a fundamental support to improve active safety, i.e., accident prevention, by making information available beyond the driver’s (or other car sensor’s, e.g., radar) horizon of awareness with almost minimal latency. Note that active safety is composed of sensing and communication activities. In this paper, we are concerned with active safety-related communications.

When considering safety-related communication, two types of messages can be identified: periodic and event-driven. Periodic exchange of ‘status’ messages containing the vehicle’s position, speed, etc. (also called beacons in the following) can be used by safety applications to detect potentially dangerous situations for the driver (e.g., a highway entrance with poor visibility). It is assumed that every equipped vehicle will also contain a GNSS (Global Navigation Satellite System), e.g., GPS, in order to determine its absolute position. On the other hand, when an abnormal condition (e.g., an airbag explosion) or an imminent peril is detected by a vehicle, an event-driven message (also called emergency message in the following) is generated and disseminated through parts of the vehicular network with the highest priority.

While, from a safety perspective, a key challenge for direct vehicle-to-vehicle communication technologies in the market introduction phase will be to achieve a significant penetration rate of equipped vehicles, it will be challenged even more deeply in fully deployed, high density vehicular scenarios, due to the high data load on the channel solely caused by beaconing. With CSMA, a high load on the channel is likely to result in an increased amount of packet collisions and, consequently, in a decreased ‘safety level’ as seen by the active safety application. Specifically, beacon messages will not be successfully decoded even when sent by a nearby vehicle and event-driven messages will show a slow-unreliable dissemination process. To counter the issue of channel saturation, we proposed to make use of packet-level interference management based on per-packet transmit power control to give packets ‘relative’ weights that control the introduced interferences and — implicitly — the ability to capture packets.

In this paper, we analyze vehicle-to-vehicle communica-
tion from an active safety perspective and identify the challenges and required strategies to improve performance through packet-level interference management. We start by observing that with the proposed technology, i.e., IEEE 802.11p [5], the load on the wireless medium resulting from periodic message exchange should be carefully controlled in order to prevent deterioration of the quality of reception of safety-related information. To this purpose, we propose a distributed transmission power control strategy called D-FPAV (Distributed Fair Power Adjustment for Vehicular environments) that controls the beaconing load under a strict fairness criterion that has to be met for safety reasons. D-FPAV also allows a clear prioritization of event-driven over periodic messages. We then turn our attention to fast and effective dissemination of event-driven emergency messages. We design a contention-based strategy called EMDV (Emergency Message Dissemination for Vehicular environments) that ensures fast and effective dissemination of alerts in a target geographical area in cooperation with D-FPAV. Finally, we evaluate the performance of the protocols in a highway traffic scenario with the use of a significantly extended version of the ns-2 [6] simulator that has been improved to account for the IEEE 802.11p draft as well as for more realistic propagation and interference patterns. Simulation results clearly show that i) D-FPAV can successfully control the beaconing load on the channel while ensuring that the probability of beacon reception is still high within the safety distance to the sending vehicle, ii) D-FPAV significantly increases the probability of one-hop reception of event-driven messages for all distances to the sender, and iii) when used in combination with D-FPAV, the EMDV protocol achieves a fast and effective dissemination of event-driven messages. The proposed suite of protocols provides a comprehensive solution for active safety communications in IEEE 802.11-based vehicular networks.

The remainder of this paper is structured as follows: Section II identifies the communication challenges that exist in IEEE 802.11-based vehicular environments. Furthermore, it defines the goals that communication strategies for sending beacons as well as for sending emergency messages should accomplish. Section III presents recent studies most relevant to our work. Section IV defines formally the basis of our strategy to maintain the beaconing load under control, D-FPAV, that is also formally proven to achieve fairness among sending vehicles. In Section V, we propose the EMDV method to quickly and effectively disseminate emergency information within a geographical area. The simulator setup and configuration as well as the modules that we developed to enhance the simulator are given in Section VI. The performance evaluation of the proposed protocols is presented in Section VII. Finally, Section VIII summarizes the main results and presents an outlook on future work.

In this work great care has been taken to analyze thoroughly the challenges of power control as well as the proposed solution under realistic assumptions (in particular with respect to mobility, radio propagation, interferences, and protocol details of IEEE 802.11p). At the same time, a formal and rigorous treatment of the challenges and of the proposed solutions is presented. However, a parameter estimation problem occurs to bridge the gap between the rigorous treatment and the practical application for which we derive and evaluate an estimation procedure. We, therefore, start with the more formal treatment in Sections IV and V and move to a simulated assessment of realistic assumptions in Sections VI and VII. The results show that desired features can be maintained when moving from the formal treatment to realistic assumptions.

II. IDENTIFYING CHALLENGES & DEFINING GOALS

As outlined in the introduction, safety applications can be enabled by two types of messages: periodic and event-driven. Periodic status messages are intended to exchange state information from the sending vehicle, i.e., position, direction, speed, etc., and possibly also aggregated information of the surroundings. Through this beaconing activity, safety applications acquire an accurate knowledge of the surroundings and, therefore, are capable of detecting potentially dangerous situations for the driver.

The key challenge related to this beaconing activity is to control the channel load to avoid channel congestion. This assessment is supported by the following facts. As defined by the FCC (Federal Communications Commission of the USA) [7], we assume the existence of a single, 10 MHz wide channel where only safety information is exchanged.\(^1\) The data rates provided by IEEE 802.11p [5] range from 3 to 27 Mbps, where the lower ones are to be preferred for safety applications due to their robustness against noise and interferences [8]. The channel access mechanism of IEEE 802.11 systems, the Distributed Coordination Function (DCF), is an asynchronous approach unable to utilize the wireless medium efficiently. According to previous studies [9], [10], and the VSC (Vehicle Safety Communications project) final report [11], it is envisioned that several messages per second from each vehicle will be needed to provide the required accuracy for safety applications. Furthermore, additional transmission repetitions could be considered to overcome the effects of packets losses due to collisions and fading. Finally, according to recent studies [12], safety-related messages will be relatively large, between 250 and 800 Bytes, due to security-related overhead (e.g., digital signatures and certificates). A back-of-the-envelope calculation easily shows that, for example with 100 neighboring nodes sending 10 packets per second each of size 500 Bytes, the generated load can be much higher than the available bandwidth (3 Mbps with the most robust modulation/coding scheme).

In a previous study [13], we evaluated the reception rates of periodic broadcast messages in a setup as described above for different configurations of transmission power and packet generation rate. On the one hand, the results of our evaluation show that, as expected, increasing the generation rate of beacon messages decreases the probability of successful reception of each of them. On the other hand, we observed that while increasing the transmission power extended the communication range to further distances, it could also lead to a congested wireless medium where reception rates for vehicles close to the sending vehicle decreased due to packet collisions.

\(^1\)Such a channel has been coined a HALL channel (High Availability Low Latency).

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Fig. 1. Illustration of the expected probability of successful reception of period and event-driven messages in case the communication behavior and the resulting channel load is uncontrolled. In comparison, the performance of periodic and event-driven messages is shown as it should be achieved by active packet-level interference management.

Section VII presents the simulation results of configuring different transmission power values for beacon messages.

Accounting for these observations, we propose to fix the packet generation rate at the minimum required by safety applications, and to adjust the transmission power of beacons in case of congestion. This mechanism should keep the load on the wireless medium below a certain level, called Maximum Beaconing Load (MBL) in the following. To illustrate our design goal, we schematically show in Figure 1 the communication performance that can be achieved by applying packet-level interference management based on transmit power control to all periodic message transmission. Without control of the channel load, the probability of successful message reception will already drop significantly at close distances and emergency messages will not experience a better reception performance than periodic messages. On the other hand, controlling and managing the interference introduced by periodic beacon messages, as illustrated in Figure 1, the desired performance for active safety related communications can be achieved: periodic messages experience a high reception probability at close distances and event-driven emergency messages achieve an enhanced performance. Consequently, we might need to accept lower reception probabilities for periodic messages at further distances. Note that the transmit power control mechanism must be fully distributed and be able to react quickly to the very dynamic topologies of vehicular networks. Additionally, strict fairness must be guaranteed since it is very important that every vehicle has a good estimation of the state of all vehicles (with no exception) in its close surroundings. More specifically, a higher transmit power should not be selected at the expense of preventing other vehicles from sending/receiving their required amount of safety information. In Section IV, we propose D-FPAV, a distributed strategy to adjust the transmission power of periodic messages inspired by a max-min principle: the minimum of the transmission power of vehicles has to be maximized while confining the beaconing load below MBL.

Contrary to beacons, event-driven messages follow a reactive strategy, i.e., they are issued when a hazard has been detected. Event-driven messages need to be quickly and effectively disseminated within the geographical area where the danger can be a threat. The main challenge for the information dissemination scheme is related to the fact that event-driven messages will share the wireless channel with periodic messages. As a consequence of this, in case of high vehicular traffic density a high data load will be experienced on the channel, which in turn can result in longer channel access time and an increased number of packet collisions, see [13]. Furthermore, vehicular networks are a challenging environment with respect to radio wave propagation due to a high number of reflecting mobile obstacles able to randomly degrade the strength of the received signal (see [14], where the analysis of empirical data is summarized).

In Section V, we propose EMDV, a strategy to disseminate emergency information within a geographical area with short delay. EMDV has been designed taking into account probabilistic radio propagation characteristics and potentially high channel load. For safety reasons, information dissemination and beaconing need to be ‘correctly’ balanced. As a basis, a prioritized channel access mechanism, e.g., EDCA (Enhanced Distributed Channel Access) [15] as suggested in IEEE 802.11p draft, should be used to reduce the channel access time for event-driven emergency messages. On top of that, we propose to use D-FPAV to adjust (through the MBL parameter) the amount of bandwidth available for unexpected emergency information, thereby increasing the probability of successful emergency message reception.

III. RELATED WORK

Periodic one-hop broadcast communications are the basic mechanism to support safety applications, and their performance has been addressed in several vehicle-to-vehicle communication studies. In this context, Xu et al. [9] identify ‘infeasible regions’ (situations) where potential safety applications requirements cannot be satisfied due to technological limitations. Their assessment is based on an evaluation of the performance of several layer-2 repetition strategies in terms of number of updates per period of time and probability of reception failure for different fractions of channel capacity assigned to this type of messages. In a previous work [16], we studied the probability of successful reception with respect to the distance from the transmitter of periodic IEEE 802.11 one-hop broadcast messages in vehicular scenarios. Additionally, the effects of a probabilistic radio propagation model as well as the EDCA (Enhanced Distributed Channel Access) scheme suggested in IEEE 802.11p were shown. The results demonstrated that the CSMA/CA approach is highly challenged when coordinating broadcast transmissions in high vehicular traffic density scenarios with probabilistic propagation phenomena. Furthermore, the study confirmed the beneficial effect of EDCA on channel access time for messages with higher priorities.

However, to the best of our knowledge, none of the existing approaches aims at controlling the load on the wireless channel where safety-related information exchange will take place. Furthermore, congestion control strategies designed for non-vehicular environments do not address the specific challenges
of vehicular networks due to their different goal, e.g., commonly focusing on unicast flows for end-to-end connections.

Existing power control studies in the field of mobile networks frequently intend to maximize overall system capacity, energy consumption or connectivity for point-to-point communications and are not, therefore, applicable to vehicular networks; see the work of Kawadia and Kumar [17] for a description of the design principles of power control in wireless ad hoc networks. The increasing interest caused by the potential of vehicle-to-vehicle has encouraged some researchers to adopt conventional power control or fairness approaches to vehicular environments. In this group Artimy et al. [18] and Wischhof et al. [19] propose a power control scheme to maximize connectivity and a utility fair function to share the broadcast medium, respectively. Although the proposed strategies could be perfectly valid when focusing on non-safety applications, they still fail to satisfy all the safety constraints outlined in Section II.

With respect to information dissemination, we can find several strategies in the field of vehicle-to-vehicle communication that take advantage of the existence of positioning systems, e.g., GPS, to improve simple flooding. These approaches are designed according to different criteria corresponding to different types of applications and environments.

On the one hand, there is a group of studies which address non-safety applications and, therefore, are not designed according to strong reliability constraints and provide little or no attention to a reduction of the delay experienced during the dissemination process. These schemes, e.g., [20]–[24] and [25], intend to deliver information over large distances, from several kilometers to complete cities. Also, there are non-safety information dissemination schemes addressing smaller areas, e.g., to enable cooperative driving, such as [26].

On the other hand, several proposals exist which consider time-critical safety applications such as [27]–[29] and [30], which intend to deliver the information to all vehicles within local areas (up to a couple of kilometers) with low delay. Durrusi et al. propose in [27] to construct a hierarchical structure among cars driving in the same direction to manage efficiently the dissemination process. However, highly dynamic topologies would not be supported, e.g., with cars entering or leaving the road. Sormani et al. [28] suggest selecting message forwarders by the use of a probabilistic scheme, which is not proven to be a valid approach to deliver time-critical information reliably.

The authors of [29], [30] propose interesting schemes to disseminate the emergency information in a certain direction making use of contention periods, i.e., after a message transmission all receivers wait a certain time before forwarding the message. Briesmeister et al. [30] favor the re-transmission of receivers located at further distances from the sender by the selection of shorter waiting times. Biswas et al. [29] select random waiting times and utilize an implicit acknowledgment scheme to cancel re-transmissions from nodes closer to the danger (where the message originated).

Our proposal for information dissemination described in Section V makes use of the two latter principles (from [29], [30]) and further complements them with mechanisms aimed at reducing dissemination delay and improving reliability, specially in high channel load conditions.

Furthermore, contrary to the studies cited above, we consider probabilistic radio propagation on a per-packet basis for the evaluation of our protocols. Although recent channel characteristic studies such as [31]–[36] have shown that the wireless channel for inter-vehicle communication at 5.9 GHz is subject to frequency- and time-selective fading, we assume that these effects can be taken care of by 802.11p. For instance, the experienced Doppler spreads up to 2 kHz and RMS delay spreads around 0.8 µs due to multi-path radio propagation are handled by an increased guard interval of 1.6 µs between successive OFDM symbols and an intercarrier spacing of 156.25 kHz [32], [33]. Without these adaptions, which are part of the drafted 802.11p standard, the communication would be vulnerable to inter-carrier interference (ICI) and inter-symbol interference (ISI). We are also aware of the fact that multi-path propagation and high vehicular mobility causes a variation of the channel condition over time, by which, depending on the used symbol rate and the size of a packet, channel estimations which were performed at the beginning of a transmission may become invalid at the end of the packet. Though this problem is not covered by the current 802.11p draft explicitly, various proposals on how to overcome this impairment exist. The approach in [32], for instance, suggests using an advanced receiver in which a time-domain channel estimation and a frequency-domain channel tracking is performed to equalize the channel. According to the authors, this proposal has already been implemented, being completely 802.11p compliant, and evaluated in more than 300 field trials. A different solution from Zhang et. al applies differential modulation, such as DPSK, to mitigate the frequency-selective channel fading [37].

IV. FAIR CONGESTION CONTROL

In this section, we present the D-FPV (Distributed Fair Power Adjustment for Vehicular environments) algorithm, which makes use of transmit power control to achieve the following design goals:

\( i \)
congestion control: limit the load on the medium produced by periodic beacon exchange;

\( ii \)
fairness: maximize the minimum transmit power value, over all transmission power levels assigned to nodes forming the vehicular network, under constraint \( i \);

\( iii \)
prioritization: give event-driven emergency messages higher priority compared to the priority of periodic beacons.

As explained in the following, the congestion control requirement \( i \) is applied only to beacon messages, which is coherent with our design goal of controlling the channel bandwidth assigned to periodical, safety-related messages. Note that when event-driven messages are also contending for the channel, this condition might be violated at some nodes, which is perfectly fine since in our proposed framework the entire channel bandwidth is to be used in case a situation of immediate peril is detected. Concerning goal \( iii \), we anticipate that prioritization is achieved through the EDCA
mechanism available in IEEE 802.11p, and by always sending an event-driven emergency message using the maximum possible transmit power.

In the following, we first present some definitions and a description of the network model. Second, we introduce the formal definition of the beaconing problem and the designed algorithm to solve the problem assuming ideal conditions. Last, we address the estimation approaches required to implement a feasible solution for realistic environments. The resulting trade-offs and the corresponding performance evaluation is presented in Subsection VII-B.

Assume a set of nodes $N = \{u_1, \ldots, u_n\}$ is moving along a road modeled as a line\(^2\) of unit length, i.e., $R = [0, 1]$. Each of the network nodes periodically sends a beacon with a predefined beaconing frequency $F$, using a certain transmit power $p \in [P_{min}, P_{max}]$, where $P_{min}$ ($P_{max}$) denotes the minimum (maximum) transmit power.

**Definition 1 (Power Assignment):** Given a set of nodes $N = \{u_1, \ldots, u_n\}$, a power assignment $PA$ is a function that assigns to every network node $u_i$, with $i = 1, \ldots, n$, a value $PA(i) \in (0, 1]$. The power used by node $u_i$ to send the beacon is $PA(i) \cdot P_{max}$.

**Definition 2 (Carrier Sensing Range):** Given a power assignment $PA$ and any node $u_i \in N$, the carrier sensing range of $u_i$ under $PA$, denoted $CS(PA, i)$, is defined as intersection between the commonly known CS range\(^3\) of node $u_i$ at power $PA(i) \cdot P_{max}$ and the deployment region $R$. The CS range of node $u_i$ at maximum power is denoted $CS_{MAX}(i)$.

Given a power assignment $PA$, the network load generated by the beaconing activity under $PA$ is defined as follows:

**Definition 3 (Beaconing Load under PA):** Given a set of nodes $N$ and a power assignment $PA$ for the nodes in $N$, the beaconing network load at node $u_i$ under $PA$ is defined as:

$$BL(PA, i) = |\{u_j \in N, j \neq i : u_i \in CS(PA, j)\}|,$$

where $CS(PA, j)$ is the carrier sensing range of node $u_j$ under power assignment $PA$.

Informally speaking, beaconing load is measured in terms of the number of nodes that contain node $u_i$ in their CS range. In fact, under the assumptions that the beaconing frequency is fixed to the same value for all the nodes, and that beacon messages have the same size, the observed channel load is a function of the number of nodes in the surroundings. Note that the above definition of beaconing load can be easily extended to account for different beaconing frequencies in the network, and for beacon messages of different sizes.

Formally speaking, the goal of D-FPAV is to solve the following problem in a fully distributed environment:

**Definition 4: (Beaconing Max-Min Tx power Problem (BMMTxP)):** Given a set of nodes $N = \{u_1, \ldots, u_n\}$ in $R = [0, 1]$ and a value for the maximum beaconing load $MBL$, determine a power assignment $PA$ such that the minimum of the transmit power used by nodes for beaconing is maximized, and the network load experienced at the nodes remains below the beaconing threshold $MBL$. Formally,

$$\max_{PA \in PA} \left( \min_{u_i \in N} PA(i) \right)$$

subject to

$$BL(PA, i) \leq MBL \quad \forall i \in \{1, \ldots, n\},$$

where $PA$ is the set of all possible power assignments.

Note that solving BMMTxP addresses the design goals $i)$ and $ii)$ at the beginning of this section, where $MBL$ is used to control the congestion generated by beaconing activity. As simulation results in Section VII will show, goal $iii)$ can be achieved by transmitting beacons using the transmit power computed by D-FPAV, and by transmitting event-driven emergency messages at full power.

The proposed D-FPAV algorithm is based on the FPAV algorithm [38], a centralized algorithm for solving BMMTxP assuming global knowledge (node positions). FPAV itself is based on a ‘water filling’ approach [39]. Node power levels are iteratively increased by the same amount $\epsilon \cdot P_{max}$ starting from the minimum level, and this process is continued as long as the condition on the maximum beaconing load ($MBL$) is satisfied. When the process stops, all nodes have increased up to the same power level. Notice that in a previous work [38] we proposed a ‘second stage’ of the FPAV algorithm in order to achieve per-node maximality. At the second stage, specific nodes could further increase their transmission power until no node was able to increase without violating the condition on beaconing load, in accordance with the formal definition of max-min fair allocation as in [39]. However, simulation experiments where global knowledge was assumed showed that the second stage could only achieve a marginal gain in scenarios with high network dynamics [38]. Because of this, and due to the higher complexity, which implementing per-node maximality would add to the distributed protocol, the second stage of the algorithm is not considered here.

D-FPAV is based on $i)$ executing the FPAV algorithm at each node with the information gathered from received beacons, $ii)$ on exchanging the locally computed transmit power control values among surrounding vehicles, and $iii)$ on selecting the minimum power level amongst the one computed locally and those computed by the surrounding vehicles. Algorithm D-FPAV is summarized in Figure 2. A node $u_i$ continuously collects information about the status (current position, velocity, direction, and so on) of all the nodes within its $CS_{MAX}$ range. These are the only nodes that node $u_i$ can affect when sending its beacon. Since the communication range\(^4\) is typically smaller than the CS range, a strategy based on multi-hop information propagation is needed to obtain the information from nodes outside of the communication range.

\(^2\)Modeling the road as a line is a reasonable simplification in our case since we assume the communication ranges of the nodes to be much larger than the width of the road.

\(^3\)The CS (Carrier Sense) range, in ideal conditions, is the distance to which a node’s transmissions can be sensed and, therefore, prevents other nodes from accessing the channel at this time.

\(^4\)Communication range is defined in this paper as the distance where the received signal power of a transmitted message matches, on average, with the minimum power specified in order to receive a message successfully.
Algorithm D-FPAV: (algorithm for node \( u_i \))

**INPUT:** geographical positions of all nodes in \( CS_{MAX}(i) \)

**OUTPUT:** a power setting \( PA(i) \) for node \( u_i \), such that the resulting power assignment is an optimal solution to BMMTxP

1. Based on the geographical positions of all nodes in \( CS_{MAX}(i) \), use FPA to compute the maximum common transmit power level \( P_t \) s.t. the MBL threshold is not violated at any node in \( CS_{MAX}(i) \)
2a. Disseminate \( P_t \) to all nodes in \( CS_{MAX}(i) \)
2b. Collect the power level values computed by nodes \( u_j \) such that \( u_j \in CS_{MAX}(j) \) and store the received values in \( P_j \)
3. Assign the final power level:
   \[ PA(i) = \min \{ P_t, \min_{u_j \in CS_{MAX}(j)}(P_j) \} \]

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**Fig. 2.** The D-FPAV algorithm. Note that in order to disseminate/collect information to/from nodes outside the communication range multi-hop communication is involved (steps 1, 2a and 2b).

range. Various alternatives for implementing this strategy are discussed later in this section. Based on the status of all nodes within \( CS_{MAX} \) range, node \( u_i \) makes use of FPA to compute the maximum common transmit power level \( P_t \) of the transmit power for all nodes in \( CS_{MAX}(i) \) such that the condition on the MBL is not violated (step 1). Note that this computation is based on local information only (the status of all the nodes in \( CS_{MAX}(i) \)), and it might be infeasible (i.e., it might violate the condition on MBL at some node) globally. To account for this, node \( u_i \) delivers the computed common power level \( P_t \) to all nodes in \( CS_{MAX}(i) \) (step 2a). In the meanwhile, node \( u_i \) collects the same information from the nodes \( u_j \) such that \( u_i \in CS_{MAX}(j) \) (step 2b). Knowing the power levels computed by the nodes in its vicinity, node \( u_i \) can assign the final transmit power level, which is set to the minimum among the value \( P_t \) computed by the node itself and the values computed by nodes in the vicinity (step 3). Setting the final power level to the minimum possible level is necessary to guarantee the feasibility of the computed power assignment.

In the Appendix, we formally prove that, under quite idealized conditions, D-FPAV solves the BMMTxP problem within one round of communication, i.e., the time between two successive broadcast transmissions containing a node’s local power computation, and that it has polynomial time complexity. Later in this section and, more extensively, in Section VII, we show that, even in practical scenarios where these conditions are not met and where the time interval between two broadcast transmissions containing a node’s local power computation is increased, D-FPAV still provides very good performance.

Note that, while a perfect information accuracy from all nodes inside \( CS_{MAX}(i) \) is required in order to guarantee strict fairness, achieving such a perfect knowledge is very difficult in a fully distributed, fast moving scenario as given by VANETs. Furthermore, the geometric concept of a carrier sense range might even not apply in reality. While the formal treatment remains valid even with generalized definitions of \( CS_{MAX} \), the actual problem then is to estimate which nodes can be considered to be ‘in’ \( CS_{MAX} \). Hence, D-FPAV is expected to operate in situations in which nodes have incomplete knowledge about the environment (status of nodes within \( CS_{MAX} \)). Under these conditions, D-FPAV is not guaranteed to provide strict fairness. However, as the simulation results presented in Section VII show, D-FPAV is very effective in achieving a very close approximation to fair power control even if knowledge of the environment is inaccurate.

Another facet of the problem of estimating which nodes are in \( CS_{MAX} \) is given by a trade-off between information accuracy and additional overhead on the channel. Clearly, the only option to acquire status information from nodes located outside the communication range is making use of a multi-hop strategy, i.e., nodes re-transmit the status of their neighbors. To determine this strategy, the following design decisions have to be made: how often the neighbors’ status should be forwarded, what range of neighbors must be included, and which transmission power must be used to transmit this information.

We propose to put together the \( P_t \) values with the status information of the corresponding nodes inside \( CS(i) \) range\(^5\) and then, to improve efficiency, to piggyback this aggregated information in beacon messages ("extended beacons").

Now, decisions have to be made on how often the aggregated information should be piggybacked in the beacons, and which transmit power should be used to send extended beacons. In making these choices the trade-off exists between additional overhead on the channel and accuracy of the neighbor’s status information available at the nodes. In order to select the better option, we evaluate three different configurations in Section VII: piggyback the aggregated status information of 1) each beacon, 2) every 5th beacon or 3) every 10th beacon and transmit it with power \( PA(i) \) (the transmit power value as computed by D-FPAV). We considered that sending piggybacked beacons with a lower frequency than one every 10 beacons would cause D-FPAV to deal with information that is too outdated.

Finally, the issue of how fast D-FPAV reacts to changes in the vehicle density (and, hence, of the offered channel load) is of interest. From a theoretical viewpoint, we prove in the Appendix that D-FPAV computes an optimal solution to BMMTxP within the time of two successive periodic beacon transmissions, i.e., the time of two successive broadcast transmissions containing a nodes local power computation. This result holds under the assumption that the offered channel load does not change during this time, which might not be the case in a practical scenario. Similarly to the case of imperfect knowledge of number of nodes within \( CS_{MAX} \), sub-optimal transmit power allocations are to be expected in the presence of changing load conditions, leading to some performance degradation with respect to optimal, idealized conditions. However, the extensive simulation results reported in this paper and in [41] show that, also in practical scenarios, D-FPAV achieves a quite accurate and stable control of the

\(^5\)Unlike in our previous work [40], the choice of \( CS(i) \), instead of \( CS_{MAX}(i) \), has been adopted in order to achieve a lower overhead in areas with high load on the channel. Although a smaller amount of potential surrounding vehicles can be discovered, a lower overhead benefits the performance of the beacons activity, as we can see in the results shown in Section VII.
beaconing load, indicating that the rate of change in traffic load conditions is indeed expected to be lower than the frequency of information update used supporting computation of the power assignment.

V. DISSEMINATION OF EMERGENCY INFORMATION

The second main goal identified in Section II is the dissemination of event-driven emergency information within a geographical area. To deliver a message\(^6\) containing information about an existing threat an effective strategy offering short delay is required.

We assume that a vehicle detecting a hazard issues an event-driven emergency message to warn the drivers approaching the danger. The originating node, according to the corresponding safety application, specifies the relevant area for dissemination of the alert (dissemination area). The alert must be distributed in the complete area, i.e., up to the border of the dissemination area (see Figure 3), possibly via multi-hop transmissions, with high reliability and short delay. In this paper, we study the case where roads do not comprise any intersection (or highway entry/exit), and make the reasonable assumption that the communication range of an emergency message is larger than the road’s width. The protocol proposed in this paper can be extended in order to disseminate the emergency message in two opposite directions and to support road junctions, e.g., with smart strategies such as those proposed in [42] or with the use of digital maps, which is left to future work.

The main purpose of our dissemination strategy is to select the appropriate nodes to forward the message efficiently in the direction of dissemination, to cover the entire dissemination area. The proposed strategy needs to overcome the different challenges existing in a vehicular environment, such as dealing with uncertainties resulting from node mobility, fading phenomena and packet collisions. Furthermore, since the wireless channel is utilized also for periodic beacon exchange, a relatively busy medium can be encountered by event-driven emergency messages in dense vehicular traffic situations.

In previous studies [43], [44], we showed the satisfactory performance of a forwarding strategy based on the use of the geographical positions of the nodes combined with a contention-based approach. According to this strategy, and in order to overcome the uncertainties on message reception

\(^6\)Unless otherwise stated, in this section by ‘message’ we mean ‘event-driven emergency message’.
based approaches by a limitation of the ‘contention’ range, i.e., the forwarding range in our case. These message duplicates are the result of poor reception rates of broadcast messages at distances close to the Communication Range, as we experience in our vehicular scenarios (see Section VII-A).

EMDV is composed of four main procedures, as shown by the pseudo-code description of the protocol in Figure 5. A node transmitting an emergency message invokes the PrepareMessage() procedure. This procedure first checks whether the message has already been transmitted for the maximum number of times (maxMessages) within the node’s forwarding area. If not, the FindNextHop() procedure is invoked to determine the message’s destination node. Note that this address is used only for (possibly) selecting a specific forwarder and speed-up message propagation, but the message sent to the channel still has the broadcast address specified at link layer. This ensures that every node that receives an emergency message passes it to the upper layers, and that no acknowledgment is issued for a received message. Once the message has been transmitted, the message counter is increased, and a contention period is started to verify that at least one neighbor is forwarding the message. Procedure FindNextHop() essentially scans the neighbor table of the sender to find (if any) the neighbor in the sender’s forwarding area with the highest progress in the direction of dissemination. If no neighbor in the dissemination direction can be found, or if the sender’s forwarding area is at the border of the dissemination area (see Figure 3), no specific forwarder is selected, and NextHop is set to broadcastAddress.

Procedure ReceiveMessage() is invoked when a node receives an emergency message, and first ensures that the node lies inside the dissemination area in order to proceed. Then, it is checked whether the received message has been sent by a node which is further away in the direction of dissemination and lies inside the own forwardingArea. In this case, the message can be considered as a sort of ‘implicit ack’ of message forwarding and the corresponding message counter is increased so that contention for forwarding the message can be canceled if enough ‘implicit acks’ have already been received. If the above conditions are not satisfied and the receiving node is located inside the forwardingArea of the sender, the dissemination criteria is used to determine whether immediate or contended forwarding will be performed: if the receiving node is indicated as the intended forwarder in the NextHop field, then the message is forwarded with no contention by invoking procedure PrepareMessage(); otherwise, a contention period is started by invoking the PrepareContention() procedure. Please note that a contention will be canceled if enough implicit acks have been received. For this to work, independent from the underlying vehicle traffic density, i.e., in both low and high density scenarios, a node will increment the corresponding message counter for each own (re-)transmission and for each (re-)transmission sent by a node inside of its own forwardingArea. Thereby the contention will be canceled if enough (re-)transmissions sent from within the own forwardingArea have been received or if the message has been repeated often enough by the node itself, e.g. when there is no possible forwarder who would be able to relay the message. Furthermore, if the load due to periodic beaconing is controlled and limited, the number of sufficient implicit acks is basically a matter of desired reliability and independent of the actual vehicle traffic density.

Finally, the protocol has to be adjusted with respect to two specific situations. First, the contention period after delivering the message to lower layers (PrepareMessage()) must take into account the time the message needs for accessing the channel and transmission. To account for this, the contention time is set to maxContentionTime + maxChannelAccessTime when flag=sent. Second, nodes located within forwardingRange from the border of the disseminationArea will act a little differently since the message must not travel further distances than borderDisseminationArea. Therefore: a) they will not select a nextHop, but instead the broadcastAddress will be utilized; and b) they will increment countMessages when receiving a message from any node that is also located within forwardingRange of borderDisseminationArea, instead of only counting the ones coming from their forwardingArea.

In the present paper, we study the performance of the protocol in challenging saturation conditions. However, EMDV
can easily be adapted to perform well also in sparse network situations. For instance, the case in which no vehicle is known in the direction of dissemination can be easily addressed either by storing the emergency message and issuing it when a beacon from a new vehicle is received, or by repeating the EMDV contention until a predefined lifetime timer expires.

VI. SIMULATION MODELING AND SETUP

In the next section, we evaluate the performance of the two proposed protocols, D-FPAV and EMDV, with the use of the network simulator ns-2.28. We first describe the simulation setup, including the scenario utilized, and the configuration of our proposed strategies. Special emphasis is devoted to the extension modules implemented into the ns-2 simulator that consist of more accurate propagation and interference models, realistic vehicular movement patterns, and adjustments to model the current IEEE 802.11p specifications.

A. The Network Simulator

The utilization of appropriate models and their correct configuration is a critical aspect in the evaluation of wireless communications. Furthermore, and as pointed out in existing studies, e.g., [45], although ns-2 [6] is a widely used network simulator it shows (in its standard release) insufficient accuracy in the lower layers of its wireless modules. Thus, we have modified and extended many models of the standard distribution of ns-2.28 to provide our simulations with a higher level of fidelity with respect to reality and, moreover, to model the current development status of vehicle-to-vehicle communications technology. In the following, we briefly describe the main enhancements.

First, the interference and reception model has been extended with cumulative noise capabilities. The original ns-2.28 code does not keep track of all ongoing messages at a node’s interface, i.e., it does not accumulate the power level of all ongoing interferences. As other network simulators already do, e.g., GloMoSim [46], we accumulate the power of all interfering signals together with the existing background noise \( \text{Noise} \), to determine whether the reception of a message is successful. Moreover, we also modified the capture feature since the standard distribution of ns-2.28 only allows a message to be captured if it arrives when the channel is idle. According to current wireless chipsets’ capabilities [47], our implementation also allows the successful reception of a message that arrives during a busy period of the channel as long as the following inequality is satisfied during the complete reception time\(^7\):

\[
P_r \geq I + C_p Th,
\]

where \( P_r \) is the power of the received message, \( I \) corresponds to the cumulative power level of all existing interferences plus \( \text{Noise} \), \( C_p Th \) is the capture threshold, and all powers are expressed in dB. To have a higher level of accuracy, we take into consideration all signals arriving at the interface with a power higher than \( \text{Noise} \), instead of discarding signals below \( C_p Th \) as in the original ns-2.28. The finite state machine implemented to model cumulative noise has been validated by setting up a table of all possible combinations of triggers and conditions for each state, eliminating non-feasible combinations and determining the finite state machine’s transactions to the remaining ones. Since these modifications have recently been merged into the official ns-2 tree and are publicly available as part of the ns-2.33 release, we refer either to [48] or [49] for further details.

With respect to the medium access control layer, we thoroughly analyzed and bug-fixed the ad hoc channel access mechanism (see [50]) according to the IEEE 802.11 standard [51] (which is inherited by IEEE 802.11p). With respect to the physical layer, ns-2.28 models a Lucent WaveLAN 802.11 DSSS (Direct Sequence Spread Spectrum) radio interface. To model a WAVE OFDM system, which operates at 5.9 GHz with 10 MHz channels, several modifications were required according to the IEEE 802.11a [52] standard and the IEEE 802.11p [5] draft. Independently from the data rate used to transmit a message payload, the preamble and the PLCP header are always transmitted using the lowest data rate, 3 Mbps. The modulation scheme that provides 3 Mbps is the most robust one, Binary Phase Shift Keying (BPSK) with the lowest coding rate (1/2). However, note that 16 service bits of the PLCP header are transmitted with the payload data rate, instead of the basic rate, and that padding and tail bits are added to fill up the last symbol of a message. Additionally, the slot time parameter is adapted to support larger communication distances. Again, we refer the reader to [48], [49] for a detailed report on the implementation issues. Table I presents the main parameters configured in our version of the simulator for a data rate of 3 Mbps, which is the one used to illustrate the performance evaluation of the proposed protocols.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Frequency</td>
<td>5.9 GHz</td>
</tr>
<tr>
<td>Data rate</td>
<td>3 Mbps</td>
</tr>
<tr>
<td>RTS/CTS</td>
<td>-94 dBm</td>
</tr>
<tr>
<td>CTS</td>
<td>3 dB</td>
</tr>
<tr>
<td>CSTh</td>
<td>-96 dBm</td>
</tr>
<tr>
<td>Noise</td>
<td>-99 dBm</td>
</tr>
<tr>
<td>Antenna gain</td>
<td>0 dB</td>
</tr>
<tr>
<td>Antenna height</td>
<td>1.5 m</td>
</tr>
<tr>
<td>Slot time</td>
<td>16 µs</td>
</tr>
<tr>
<td>SIFS time</td>
<td>52 µs</td>
</tr>
<tr>
<td>Preamble length</td>
<td>32 µs</td>
</tr>
<tr>
<td>PLCP header length</td>
<td>9 µs</td>
</tr>
</tbody>
</table>

\[
\text{TABLE I} \quad \text{Ns-2.28 MAC and PHY configuration values for simulations of vehicle-to-vehicle communications.}
\]

\(^7\)According to private conversations with the electronics company Siemens within the ‘Networks on Wheels’ project [4], a packet cannot be received correctly if it arrives between 4 and 10 µs after the previous one due to resynchronization issues.
Jijun Yin et al. performed real world tests on highways, and they suggest the use of the Nakagami fading model for these type of vehicular scenarios [14], [57]. Furthermore, Taliwal et al. implemented the model into ns-2.28, which we use in this study. The Nakagami-m model derives the received signal strength from a multi-path environment where the different signal components arrive randomly because of the different propagation phenomena. It is used to estimate the signal amplitude at a given distance from the transmitter as a function of two parameters, $\Omega$ and $m$. The following expression describes the Nakagami probability density function (pdf) of the received signal amplitude $x$:

$$f_{\text{amp}}(x; m, \Omega) = \frac{2m^m}{\Gamma(m)\Omega^m}x^{2m-1}\exp\left(-\frac{m}{\Omega}x^2\right), \quad m \geq \frac{1}{2}$$

where $\Omega$ defines the average received power at a specific distance, and is set to match the two ray ground path loss of ns-2.28 in our simulations; the $m$ value identifies the fading intensity, which depends on the environment, and $\Gamma$ is the Gamma function. As illustrated in Figure 6 the probability of successful message reception is perfect up to the intended communication range if no fading is considered. With fading, the probability of successful message reception is already less than 100% within the intended communication range. Moreover, the probability of reception decreases if the fading intensity is increased. For instance, a Nakagami $m = 1$ distribution is equivalent to a Rayleigh distribution and models a rough None-Line-Of-Sight scenario, whereas for parameters $m > 1$ Nakagami models an increased Line-Of-Sight scenario. To demonstrate that our proposals are valid over a wide range of fading intensities, we have configured values of $m \in \{1, 3, 5\}$ in this study. In our evaluation, we refer to Nakagami $m = 1$ as severe fading conditions, to Nakagami $m = 3$ as medium fading conditions, and to Nakagami $m = 5$ as low fading conditions. Also, as mentioned in Section III, we assume that OFDM receivers will be able to mitigate the challenges which are imposed by the time- and frequency-selectivity of the wireless channel and therefore assume that varying received signal strengths during the reception of a single packet can be equalized.

Last, microscopic movement patterns validated with measurements of real-world German highway traffic, provided by DaimlerChrysler for the Fleetnet [58] and NoW [4] projects, were utilized, see [59]. The evaluated vehicular scenarios consist of a 6 km long bidirectional highway with 3 lanes per direction. Unless otherwise stated, we utilize a vehicular density which corresponds to an average of 11 vehicles per kilometer in each lane, traveling at an average speed above 120 km/h. Note that this scenario corresponds to free flow vehicular traffic, i.e., the vehicular density can be much higher on many real highways during several hours of the day. However, we are interested in high speed scenarios with high dynamics where the utilization of high transmission power and packet generation rates is envisioned.

Fig. 6. Probability of successful beacon reception (no interference from other transmissions) with respect to the distance when no fading (Two-Ray Ground) and Nakagami-m fading with different intensities ($m = 1, 3, 5$) is considered. The transmit power has been set to the power required to achieve a communication range of 500 m when considering the Two-Ray Ground model.

### B. Simulation Setup

In the simulated highway scenarios, all vehicles are equipped with wireless communication interfaces and generate 10 beacons per second, which is the packet generation rate required by many safety applications according to existing studies, e.g., [9] or [10]. The size of each packet is configured to 500 Bytes, as mean value suggested in security studies, e.g., [12], due to the security-related overhead (i.e., digital signature plus a certificate). The maximum communication range for beacons is configured to 1000 m according to the IEEE 802.11p standard that states that vehicular communications will occur over distances up to 1000 m between high-speed vehicles.

The data rate utilized is 3 Mbps due to the robustness of the BPSK modulation scheme (see [8]): it requires the lowest SINR (signal to interference plus noise ratio) to receive a message successfully, namely 5 dB. Additionally, the IEEE 802.11 contention window is configured to 15 slots in our simulations. Larger contention window values caused average channel access times higher than 100 ms, i.e., not all generated beacons could be transmitted to the channel.

When evaluating D-FPAV, a reference node, or originator, generates single-hop event-driven messages, one per second. When evaluating EMDV, the event-driven message is destined to a dissemination area that comprises a segment of the highway starting at the originator and going up to two kilometers opposite to the driving direction. The originator is located around kilometer 4 of our highway segment and, accordingly, the 2 km long dissemination area is located in the middle of the 6 km scenario. All event-driven messages, independent of whether D-FPAV is used or not, are sent with a CR = 1000 m. Also, event-driven messages are configured with a higher link-layer priority than beacons using the differentiated access categories (EDCA mechanism) as described in IEEE 802.11e [15].

With respect to the communication strategies, we set the maximum beaconing load (MBL) of D-FPAV to two different values, 2.5 Mbps and 2 Mbps, to evaluate the prioritization of event-driven messages over beacons. Note that here we express
the MBL threshold in terms of Mbps, instead of number of nodes within CS range as it was done in Section IV. However, the two measures are equivalent when the packet generation rate and the packet size (assumed to be the same for all the nodes) are known. We fix each neighbor entry in the neighbor table to 15 Bytes (corresponding to vehicle identifier and position) and specify that nodes delete neighbor entries from their neighbor table that are older than one second. Finally, each node will estimate its CS range for the local execution of the D-FPAV algorithm. The CS range is given by the distance at which the average path loss causes the signal strength to drop below the carrier sensing threshold, i.e., the one computed using the Two-Ray Ground model of ns-2.28. Please note that the estimated CS range is only used to calculate the expected load in the network under a specific power assignment and to determine the neighbors to be included in extended beacons. The propagation of a transmitted signal will still follow the Nakagami-m fading model.

With respect to EMDV, we fix the maxContentionTime to 100 ms and the maxChannelAccessTime to 10 ms as appropriate values for our scenario according to a study of one-hop broadcast communications, which is outlined at the beginning of Section VII-A. The forwarding range is configured to three different values, 300 m, 500 m and 700 m, in order to study the trade-off between reliability, overhead and delay. Last, we study the performance of three different values for the amount of transmissions (maxMessages) in a node’s forwardingArea, namely 1, 2 and 3.

To obtain statistical significance we simulate ten different highway scenarios, with the same average vehicle density, with ten random seeds for every selected configuration. Each simulation consists of 11 s of simulated time and the statistics corresponding to the first second of simulation are not taken into account as transitory state. All results obtained are represented with a 95% confidence interval.

The configuration details are summarized in Table II.

<table>
<thead>
<tr>
<th>PARAMETER</th>
<th>VALUE</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of lanes</td>
<td>3 × direction</td>
</tr>
<tr>
<td>Vehicle density</td>
<td>11 cars/km per lane</td>
</tr>
<tr>
<td>Average speed</td>
<td>121.36 km/h</td>
</tr>
<tr>
<td>Propagation model</td>
<td>Nakagami m ∈ {1, 3, 5}</td>
</tr>
<tr>
<td>802.11p data rate</td>
<td>3 Mbps</td>
</tr>
<tr>
<td>Contention window</td>
<td>15</td>
</tr>
<tr>
<td>Packet size</td>
<td>500 Bytes</td>
</tr>
<tr>
<td>Communication range:</td>
<td></td>
</tr>
<tr>
<td>Event-driven messages</td>
<td>1000 m /19 dBm</td>
</tr>
<tr>
<td>Beacons (without D-FPAV)</td>
<td>1000 m /19 dBm</td>
</tr>
<tr>
<td>Beacon generation rate</td>
<td>10 packets/s</td>
</tr>
<tr>
<td>D-FPAV</td>
<td>On, Off</td>
</tr>
<tr>
<td>D-FPAV MBL</td>
<td>2.3 Mbps, 2.0 Mbps</td>
</tr>
<tr>
<td>Neighbor entry size</td>
<td>15 Bytes</td>
</tr>
<tr>
<td>Dissemination area length</td>
<td>2 km</td>
</tr>
<tr>
<td>EMDV forwarding Range</td>
<td>300 m, 500 m, 700 m</td>
</tr>
<tr>
<td>EMDV maxMessages</td>
<td>1, 2, 3</td>
</tr>
<tr>
<td>EMDV maxContentionTime</td>
<td>100 ms</td>
</tr>
<tr>
<td>EMDV maxChannelAccessTime</td>
<td>10 ms</td>
</tr>
</tbody>
</table>

TABLE II
Configuration parameters for D-FPAV and EMDV evaluation.

As described above, our simulation scenario consists of a bidirectional highway where all vehicles are equipped with wireless communication systems and periodically transmit 10 packets/s (beacons). Before evaluating the D-FPAV and EMDV protocols, we study some aspects of IEEE 802.11p-based one-hop broadcast communications in vehicular scenarios. The purpose of this evaluation is to obtain valuable insights into the performance of vehicular networks, to corroborate the performance statements of Section II, and to determine appropriate values for the configuration of our protocols.

Figure 7 compares the probability of successful beacon reception, with respect to the distance between sender and receiver, for various values of CR (from 250 m to 1000 m) and two different vehicular densities. Figure 7(a) presents the results obtained with the lower vehicular density, 36 cars/km, and Figure 7(b) with the higher one, 66 cars/km. In both scenarios we considered medium channel fading conditions.

In general, increasing the transmission power of one message increases its robustness against power fluctuations as well as interference and, thus, it is capable of reaching further
distances⁸. However, increasing the transmission power of all nodes in a network increases their CS ranges and, therefore, the number of nodes sharing the channel at all locations.

We can observe that, while the channel is not saturated, i.e., when the amount of simultaneous transmissions from neighboring nodes is negligible, increasing the transmission power does not significantly decrease the reception rates at close distances, and provides improved reception rates at further ones. Indeed, no drawback due to using higher transmission power values can be observed in Figure 7(a), where the lower vehicular density is utilized.

On the other hand, a CR = 750 m in Figure 7(b) experiences a significantly higher number of collisions at close distances from the sender due to the higher level of interfering signals. Moreover, the reception rates at close distances from the sender are further reduced in case of CR = 1000 m. The reason for these low reception rates at close distances from the sender is the inability of the channel access mechanism to coordinate the high number of neighboring nodes in this scenario.

We remark that due to the kinetic energy of moving vehicles, reception rates at close distances are more relevant from a safety perspective. In case of the higher vehicular density and with a packet generation rate of 10 packets per second, a CR of, e.g., 500 m would be a better choice than 1000 m, even though a higher CR provides increased probability of reception at far distances. Therefore, lack of node transmit power control can result in a lower safety level due to the decreased reception rates experienced at close distances from the transmitters.

Further analysis on different parameter configurations in this setup assisted us in adjusting the designed protocols, as well as the modulation and contention window value of the channel access strategy, which are depicted in Table II.

B. D-FPAV Performance

In order to evaluate D-FPAV performance we consider two main simulation setups, D-FPAV On and D-FPAV Off. In D-FPAV Off simulations, all beacons are sent at maximum power (CR = 1000 m) since no power control is applied. On the other hand, in D-FPAV On simulations, beacons are sent using the transmit power as computed by D-FPAV. In this set of simulations, we fix the maximum beaconing load (MBL) to 2.5 Mbps. To study the performance in different fading environments, we have configured Nakagami-m to reflect severe, medium and low fading conditions. However, we will focus on the results obtained in medium channel fading conditions and complement them with a selected set of observations obtained in severe or low fading environments.

The main metrics considered to evaluate D-FPAV’s performance are: i) the probability of successful reception of a beacon message with respect to the distance, and ii) the average Channel Access Time (CAT). The CAT is computed for all nodes in the highway and it is used to corroborate the claim that D-FPAV reduces the load on the channel uniformly in the network, i.e., it achieves fairness. The probability of reception is used to assess D-FPAV’s effectiveness and the appropriate prioritization of safety-related messages (design goals stated in Section II), which is obtained by ensuring a high probability of correctly receiving beacons at close distances from the sender and, at the same time, by increasing the probability of successful reception of event-driven messages at all distances.

Before performing the above described experiments, we have to fix the estimation procedure with respect to obtaining information on which node is residing in the ‘carrier sense range’. As indicated in Subsection VI-B, each node will estimate its CS range as the distance given by the average path loss experienced in our simulations, i.e., the one computed using the Two-Ray Ground model of ns-2.28. We evaluate different strategies that D-FPAV can use to obtain the status information from vehicles driving inside a node’s carrier sense range (CS), as described in Section IV. Figure 8 presents the probability of successful beacon reception for the different strategies as well as with D-FPAV Off for comparison. These strategies are differentiated by the generation rate of extended beacon messages which contain not only the status information of the transmitter, but also positional information about its surrounding nodes.

Figure 8 shows the results obtained with D-FPAV Off and D-FPAV On using the different configurations of the protocol. Reception rates with D-FPAV Off present low values due to the high load existing on the wireless medium and the resulting packet collisions. Indeed, the high saturation on the wireless medium causes reception rates below 60% for nodes located at a distance of 100 m or further away. Note that the near-far effect⁹ of radio wave propagation allows higher reception rates at very close distances from the transmitter, i.e., 90% at a few meters, and causes the strong decrease up to 150 m. By adjusting the transmission power of all beacons, including the extended ones, the desired results are achieved (Figure 8): an increased probability of reception at close distances from the sender for the cases where each beacon is an extended one (denoted 1over1), where every fifth beacon is sent as

⁸Note that an analysis of message reception failures and a comparison between deterministic and probabilistic models is out of the scope of this document. We refer the reader to our previous work [60] for a detailed study.

⁹The near-far effect refers to the significantly higher received power of messages sent from close distances when compared to messages sent from further ones due to the strong decrease of radio wave power along the distance.
an extended beacon (denoted 1over5), and where every tenth beacon is sent as an extended beacon (denoted 1over10).

Comparing the three curves in Figure 8, we can see how sending a lower number of extended beacons achieves higher reception rates. Note the existing trade-off between information accuracy and the associated overhead of D-FPAV. Sending a higher number of extended beacons offers the possibility to obtain more up-to-date information about the status information from surrounding nodes (further than direct communication distances). However, the larger number of extended beacons causes a higher amount of offered load to the channel and consequently requires a further reduction of the transmission power to adhere to the MBL constraint. Note that extended beacons are significantly larger than non-extended ones. In the case of 1over10, the introduced D-FPAV overhead, due to an average extended beacon size of 1120.6 Bytes, is already 12.4%. This extended size corresponds to an average of 41.37 known neighbors within the resulting CS range, 448 m in this case (CR = 356 m).

Therefore, we conclude that sending one extended beacon every 10 transmissions presents the best trade-off between accuracy and overhead among the studied options. Note that due to the high number of nodes within the communication range of each other, the same information is repeated by several nodes. Thus, extending one beacon every 10 provides a sufficient degree of neighbor table accuracy at a lower price than 1over5 in terms of overhead. For this reason, in the following we adopt the 1over10 strategy in the D-FPAV design.

The observations up to now are also valid if we consider more or less severe fading of the wireless channel. As illustrated in Figure 9(a), the probability of successful message reception increases at close distances and decreases at far distances if D-FPAV is not used and fading is severe. Due to the greater variation of the received signal strengths which causes a reduced number of interferences from far distances, the chance to decode a message successfully is increased for close distances. At the same time, the probability is decreased for far distances. Severe fading can therefore also be seen as a natural way of performing congestion control. The same phenomenon does not occur if D-FPAV is enabled, as can be seen in Figure 9(b). Since the interference level is already controlled and limited by the D-FPAV algorithm, the probability of successful message reception decreases over all distances if the fading intensity increases. Nevertheless, comparing the curves of Figure 9(a) and Figure 9(b), the benefit of transmission power control clearly exists, also in severe fading environments.

Figures 10(a) and 10(b) present the probability of successful packet reception with respect to the distance of beacons and single-hop event-driven messages with D-FPAV On and Off under severe and medium fading channel conditions. As outlined above, not using power adjustment results in a high load experienced on the channel which, in turn, causes a high number of packet collisions and low reception rates. Note that if beacons and event-driven messages are sent with the same transmission power (D-FPAV Off), event-driven messages achieve higher reception rates at closer distances. As explained in a previous work [16], a prioritized channel access category decreases the probability to experience collisions with neighboring nodes.

Using the D-FPAV mechanism and setting the maximum beaconing load (MBL parameter) to 2.5 Mbps results in an average reduction of the beacon’s transmission power from 19 dBm to 4.9 dBm, which decreases the communication range from 1000 m to an average of 356 m. Therefore, the CS range is reduced to 448 m which, according to an average of 66 cars/km, corresponds to an average of 59.13 vehicles within the CS. Note that 59.13 vehicles correspond to an offered load of 2.36 Mbps, which is less than the MBL threshold (2.5 Mbps) due to the conservative approach of D-FPAV, i.e., the minimum of the PA values received from nodes within $C_{S_{MAX}}$ is selected (see Section IV).

To evaluate the saturation on the channel we also computed the average channel busy time ratio. As intended, the reduction of the transmission power decreases the average channel busy time ratio experienced by all nodes in the highway, from about 86.2 % with D-FPAV Off to 62.2 % with D-FPAV On, a 24 % decrease.

The resulting power adjustment allows D-FPAV to fulfill its design goal of ensuring high message reception rates at close distances from the sender, corresponding to the safety
distance of a vehicle\textsuperscript{10}. As outlined in Section II, achieving a good estimation of the close environment is critical to identify dangerous situations. In our scenario with a medium fading intensity (Figure 10(b)), beacons’ probability of successful reception presents higher values up to distances of 160 m with D-FPAV On, e.g., an increase of 41.7\% at 100 m (from 54.0\% with D-FPAV Off to 76.5\% with D-FPAV On). Additionally, we can observe a significant increase of the reception rates experienced by each transmission of an event-driven message at all distances with D-FPAV On. Experiencing a lower load on the medium allows event-driven messages, which are not restricted in terms of transmission power, to achieve improved reception rates not only at close distances (e.g., a 78.6\% increase at 100 m, from 55.7\% to 99.6\%) but also at further ones (e.g., 192.2\% increase at 500 m, from 24.3\% to 71.0\%). The price to pay for these improvements is the lower reception rates of beacons for distances further than the 160 m, which, however, are distances where the information conveyed by beacons is less relevant compared to the ‘closer beacons’ and emergency messages. In an environment with higher fading intensity (Figure 10(a)) the difference between D-FPAV On and Off is, as expected, slightly reduced for beacon messages.

\textsuperscript{10}The safety distance of a vehicle commonly refers to the distance that a driver needs to stop the vehicle completely, and it is approximately calculated (in meters) as half of the value of the speed (in km/h). For example, a car driving at 120km/h has a safety distance of approximately 60m.

Yet the probability of reception of emergency messages still benefits significantly from the load reduction of D-FPAV.

To evaluate the fairness of the algorithm we study the average channel access time of all nodes on the highway. Figure 11(a) illustrates the results obtained with medium fading conditions, where each vehicle is represented with its middle position\textsuperscript{11} during the simulation run. In this case, the results of only one scenario is presented in order not to average out different vehicular densities in different segments of our highway. We omit a detailed presentation of CAT results in severe and low fading channel conditions since the difference from the medium fading condition is only marginal.

We can observe how the average channel access time has been reduced from 17.5 ms to 1.1 ms when using D-FPAV. Furthermore, if no power control is applied, nodes can experience considerably different values of CAT, ranging from about 13 ms to 22 ms, see Figure 11(b). Since the CAT reflects the amount of load on the channel at that particular location, the results obtained with D-FPAV Off show that different nodes have different opportunities of sending and correctly receiving messages, impairing fairness. On the other hand, when D-FPAV is active all the nodes experience similar

\textsuperscript{11}We compute the middle position of a vehicle as the middle point between its position at the beginning of the simulation and its position at the end.
the emergency information reception rates up to an average of 99.9%. The result shows the dependency of the success of the dissemination strategy on the channel load conditions.

Figure 12(b) shows the probability of reception in the dissemination area obtained when setting maxMessages = 2. Note how the curve presenting the reception rates obtained with D-FPAV Off is increased with respect to the values observed in Figure 12(a) when maxMessages = 1, i.e., from 90.9% to a 99.1% on average. In order to achieve a 100% probability of reception within the dissemination area with D-FPAV Off, maxMessages must be set to 3 repetitions, see Table III(b). Indeed, we discovered that due to the high load on the channel, several dissemination processes did not succeed at all, since the initial transmission of the originator was not received by at least one of the intended receivers. As intended, allowing more message repetitions within a node’s forwardingRange enhances the reliability of the protocol and resolves that problem, but at the cost of an increased overhead.

In Table III(b), we also present the average number of retransmissions caused by the EMDV protocol, i.e., the number of times that the emergency message is transmitted by any node within the dissemination area. Observe how with D-FPAV Off and Nakagami m = 3 increasing maxMessages from 1 to 2 causes the emergency message to increase from 39.5 to 67.1 retransmissions per dissemination process, and to 87.6 in case of allowing 3 repetitions.

When using D-FPAV the most efficient EMDV choice is to configure maxMessages = 1 since it already reaches a 99.9% delivery rate while requiring fewer messages on average than the other choices, i.e., 8.1 and 16.3 messages less than configuring maxMessages to 2 and 3, respectively. However, it is the responsibility of the application designer to define the requirements for communication protocols, i.e., maxMessages 3 may be preferred due to the 100% reception rates achieved with both D-FPAV On and Off.

If we consider different fading intensities, we observe that a low fading intensity, i.e. Nakagami m = 5, presents equivalent results to Nakagami m = 3 in terms of probability of reception and number of retransmissions, see Table III(c). On the contrary, in more severe fading environments, such as...
Nakagami $m = 1$, the dissemination reliability for D-FPAV Off and maxMessages $= 1$ is higher compared to the medium fading condition. Here, the interference level and the chance of a packet to collide is decreased, resulting in an improved dissemination process and thus in a higher probability of reception within the dissemination area. However, due to the higher fading and the lower probability to successfully receive a message at further distances, the number of retransmissions is slightly increased.

Furthermore, we analyzed the effect that event-driven messages have on beacon reception rates during the complete simulation. Figure 13 presents the probability of successful reception of beacons sent by the reference node for the three values of maxMessages as well as for the case where no EMDV process is started, always with D-FPAV On. The difference between the three curves stays below 2% for all distances, showing the low impact that the emergency dissemination process has on the reception rates of periodic messages. Indeed, a simple calculation of the additional load required by each dissemination process shows, that with the configured emergency message size of 500 Bytes and a retransmission count between 15 and 30, see Table III, in each dissemination process only up to 15 KB/bytes of data will be sent in total. Since the total amount of data is transmitted within about 20 ms, and taking into account some degree of spatial reuse (due to the large dissemination area), a 'peak bandwidth utilization' of 375 KB/second can be expected for the dissemination process.

In the following, we focus on the performance of maxMessages $= 1$, which provides a 99.9% of delivery ratio with D-FPAV On and utilizes the least amount of overhead. Figure 14 shows the average delay experienced by the nodes in the dissemination area until receiving the emergency information with respect to the distance to the originator. Both curves present higher values for increasing distances, as expected due to the multi-hop dissemination approach. In case of D-FPAV Off, event-driven messages are disseminated up to 2 km with an average delay below 250 ms. This delay should be compared to the estimated driver reaction time, which is on the order of 700 ms and higher [61]. Furthermore, in case D-FPAV is utilized, the delay experienced falls significantly: from 52.3 ms to 4.7 ms for close distances to the sender and from 235 ms to 20 ms in case of a vehicle located 2 km away from the originator. With respect to different fading intensities, we observed different delays only for the D-FPAV Off case, i.e., for $m = 1$ the average delay went up to 290 ms and for $m = 5$ down to 226 ms. The delays when using D-FPAV On changed only slightly by 1 ms.

Another relevant parameter for safety is the maximum delay experienced by the information to be delivered. To account for this, we measured the maximum time of all simulated scenarios that a node located at 2 km of the originator, i.e., at the other edge of the relevant area, has to wait until receiving the emergency information. According to the results obtained, the maximum delay experienced in case of D-FPAV Off is 924 ms, whereas in case of D-FPAV On it is only 80 ms. Note the difference of 844 ms between both cases, which is a significant value when compared to the driver reaction time mentioned above. Finally, we study the performance results obtained with a forwardingRange of 300 and 700 m, see Table IV. Let us focus on the values obtained with D-FPAV Off first, where the channel load is not controlled. We can observe how the reception rates vary between 91% and 93% in all cases. With respect to delay and amount of retransmissions, configuring a forwardingRange of 300 m presents the worst results, due to the limitation of the number of possible forwarding nodes and a highly saturated wireless environment. The cases of 500 m and 700 m do not present

\[\begin{array}{|c|c|c|c|c|c|c|c|}
\hline
\text{forwardingRange} & \text{300 m} & \text{500 m} & \text{700 m} \\
\hline
\text{D-FPAV} & \text{Off} & \text{On} & \text{Off} & \text{On} & \text{Off} & \text{On} \\
\hline
\text{Prob. reception} & 91.9% & 99.9% & 90.9% & 99.9% & 92.7% & 99.8% \\
\hline
\text{Avg. delay at 2 km} & 313 ms & 72 ms & 235 ms & 70 ms & 238 ms & 17 ms \\
\hline
\text{Retransmissions} & 47.2 & 11.6 & 39.5 & 16.2 & 37.1 & 13.2 \\
\hline
\end{array}\]
significant differences due to the low message reception probability between both distances as illustrated in Figure 10(b) (‘Event-driven D-FPAV Off’). When D-FPAV is active, on the other hand, the three values of forwardingRange achieve almost a perfect message reception within the dissemination area. In a controlled wireless channel, as expected, allowing a larger forwardingRange allows to reach the 2 km distance with fewer hops, thus presenting a shorter average delay, i.e., from 27 ms in case of a 300 m forwardingRange to 17 ms in case of 700 m. Furthermore, we can observe a higher robustness of the shortest forwardingRange 300 m, which presents the smallest number of retransmissions. Forcing shorter wireless hops decreases the probability to generate message duplicates due to the high probability of message reception up to the 300 m distance when the load is under control, see the ‘Event-driven D-FPAV On’ curve in Figure 10. The price to pay, as outlined above, is a slower dissemination speed.

D. Choice of MBL value

Finally, we evaluated the prioritization effect that a different choice of the MBL value has on both types of messages and, therefore, on the performance of our protocols. We simulated the same scenario as in the previous section with an MBL set to 2 Mbps and describe the results obtained in the following. A smaller MBL value further restricts the transmission power utilized for beacons, i.e., it achieves a more strict prioritization of event-driven messages over periodic messages. In case of configuring MBL = 2.0 Mbps (instead of 2.5 Mbps), the average transmission range of beacons is decreased to 346 m (instead of 356 m) and the channel busy time ratio to 54.4 % (instead of 62.2 %). Figure 15 presents the effect of configuring MBL with the two selected values on the reception rates of single-hop messages. We can observe how with MBL = 2.0 Mbps event-driven messages benefit from a lower load on the medium, which increases their probability of being successfully received over the distance. Note how this difference is more noticeable at far distances, i.e., from 500 m, due to the lower number of collisions resulting from hidden terminals.

With a lower MBL, the EMDV protocol achieves a more efficient performance due to the lower channel load and the increased event-driven messages’ reception rates. The probability of information reception with maxMessages = 1 and forwardingRange = 500 m obtains a 99.9% along the dissemination area, as with MBL = 2.5 Mbps. However, a lower load on the channel results in a smaller channel access time for event-driven messages in every hop, which results in an average delay of 8 ms to deliver the emergency information at 2 km from the information originator, less than half the time when compared with an MBL = 2.5 Mbps. Furthermore, the number of messages sent per dissemination process is also lower with MBL = 2.0 Mbps, 15.4 instead of 16.2.

VIII. Summary and Conclusions

This work is based on the assumption that vehicular networks will be using IEEE 802.11p, or an 802.11 variant, and that market penetration will be high. Active safety communication will consist of two types of messages, periodic beacon messages and event-driven emergency messages. We showed that channel saturation can ‘easily’ occur due to load caused by beacon message transmissions. Simply increasing rate or power will just make the channel conditions worse. In these ‘uncontrolled’ saturated channel conditions, both types of messages might not be received where they are needed and, thus, will not contribute to the original goal of improving road traffic safety.

To satisfy the requirements of active safety communication in vehicular networks also under these ‘stressed’ conditions, we have proposed two communication strategies that can be used separately but show synergistic effects when combined. On the one hand, we have proposed the D-FPAV algorithm to limit the beaconing load on the channel below a predefined threshold while ensuring a high probability of beacon reception at close distances from the sender. On the other hand, we have proposed the EMDV protocol to disseminate emergency information within a geographical area.

D-FPAV is a transmit power control approach based on a strict fairness criterion that is able to maximize the minimum value over all transmission power levels assigned to nodes forming the vehicular network under a given constraint on the maximum beaconing load. As a distributed algorithm, with D-FPAV each node V needs as input the number of nodes that are able to sense node V’s transmission. When this information is available, it can be proven that D-FPAV provides an optimal power assignment. Under realistic assumptions, the required input has to be estimated. We show via a simulative investigation that the estimation procedure is sufficiently accurate and with low communication overhead. The simulation results show that D-FPAV works very well in realistic vehicular environments.

13In [60], we showed that the impact of hidden nodes in a broadcast environment increases with the distance to the transmitter. This effect occurs due to the capability of wireless interfaces to successfully receive a signal in the presence of an interference if the latter one is weak enough, i.e., the capture feature.
The EMDV approach provides for robust and effective information dissemination of emergency information. For EMDV, we make use of the idea of contention-based forwarding that can very well deal with the unreliability of the channel and with node mobility. For reduction of the dissemination delay we also make use of beacon information and of classical position-based forwarding techniques in combination with the contention-based approach.

Synergy is gained when using both protocols together since D-FPAV can ensure that the channel load, in particular the channel busy time, is kept at a level where EMDV (or other dissemination protocols) can successfully operate.

The performance of the proposed protocols has been analyzed via simulation. For a proper evaluation we extended the network simulator ns-2 with more accurate reception, interference and propagation models, and adjusted it to the current version of the IEEE 802.11p draft. Furthermore, realistic vehicular movement patterns corresponding to fast-moving German highway scenarios were utilized.

According to the results obtained, our suite of protocols presents a viable solution for improving active safety related communications in IEEE 802.11-based vehicular networks. When we consider the two proposed approaches together with the formal treatment and with the simulative performance evaluation as the key contributions, we see the results obtained for a ‘plain’ IEEE 802.11p-based systems also as a valuable contribution for understanding the performance limits of a system without power or rate control.

For future work, many issues need to be further investigated. We will explore in detail the complete parameter space of EMDV in accordance with the environment and will address complex scenarios with intersections and with multiple information originators. Eventually, power and rate control should be jointly treated for optimum performance of the vehicle-to-vehicle communication system, especially in traffic scenarios with a very high vehicle density, e.g. in traffic jam situations. In such scenarios, for instance, it might be better to first reduce the beacon rate (since the velocity of the vehicles and the rate of topology changes is relatively small) and then reduce the transmission power to control the load on the wireless channel.

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successive periodic beacon transmissions, i.e., the time of two successive broadcast transmissions containing a node’s local power computation.

Proof: First, we have to show that, under the theorem assumptions, the power assignment computed by D-FPAV after one round of communication is a feasible solution to BMMTxP. Assume the contrary, i.e. assume there exists node $u_i$ such that $BL(PA, i) > MBL$, where $PA$ is the power assignment computed by D-FPAV. This means that node $u_i$ has too many interferers, all of which are located in $CS_{MAX}(i)$ (assuming symmetric CS ranges). Let $u_j, \ldots, u_{j+h}$, for some $h > 0$, be these interferers, and let $PA_i$ be the power assignment computed by node $u_i$ for all the nodes in $CS_{MAX}(i)$. In step 1 of D-FPAV, $u_i$ computes an optimal solution $PA_i$ to BMMTxP restricted to $CS_{MAX}(i)$. Assuming symmetric CS ranges, this solution includes a power setting for the interferers $u_j, \ldots, u_{j+h}$, and this power setting is such that $BL(PA_i, i) \leq MBL$. At step 2 of D-FPAV, the power setting $PA_i$ is disseminated to all nodes in $CS_{MAX}(i)$, which includes all the interferers $u_j, \ldots, u_{j+h}$. Hence, each of the interferers receives from node $u_i$ a power setting $PA_i$ such that the condition on the beaconing load is not violated at node $u_i$. Since the final power setting of the interferers is at most $PA_i$ (this follows from the minimum operation executed at step 3 of D-FPAV), since the number of nodes within range $CS_{MAX}$ from $u_i$ are not changed, and assuming a monotonic CS range$^{14}$, we have that the beaconing load at node $u_i$ cannot exceed the MBL threshold, leading to a contradiction. This proves that the power assignment computed by D-FPAV is a feasible solution to BMMTxP.

Let us now prove that the computed power assignment is optimal. Let $PA$ be the power assignment computed by D-FPAV after all power computations by surrounding nodes have been received, and let $p_{min}$ be the minimum of the node power levels in $PA$. Assume $PA$ is not optimal, i.e. there exists another feasible solution $PA'$ to BMMTxP such that the minimum of the node power levels in $PA'$ is $p' > p_{min}$. Without loss of generality, assume that $PA'$ sets the power level of all nodes in the network to $p'$. Since $PA'$ is feasible, we have that $BL(PA', i) \leq MBL$ for all $i$. Hence, given monotonicity of CS range, every node $u_i$ in the network computes a power setting $P_i \geq p'$ at step 1 of D-FPAV (this follows from the water-filling principle used in the FPAV algorithm). Since the solution computed at stage 1 by each node is at least $p'$, each node receives power values at least as large as $p'$ in step 2b of the algorithm. Hence, the final power setting of every node in the network as computed by D-FPAV at step 3 is at least $p' > p_{min}$, which contradicts our initial assumption that the minimum of the power levels computed by D-FPAV was $p_{min}$. It follows that the solution computed by D-FPAV is optimal, and the theorem is proved.

Theorem 2: Algorithm D-FPAV has $O(n)$ message complexity.

The straightforward proof of the theorem is omitted.

$^{14}$Under this assumption, an increase in transmit power can only increase the CS range.